Unit Overview and Guidance

- The exemplification has been taken from the NCETM online 'Resource Toolkit', with additions in order to ensure full coverage.
- Links to the White Rose Maths hubs schemes of work (with questions categorised into the three aims of the national curriculum i.e. fluency, problem solving and reasoning) are hyperlinked to each of the objectives. Many thanks go to the White Rose Maths hub for permission to include their resources.
- The NCETM reasoning questions have also been incorporated into each unit and are identified in pale purple boxes underneath the group of the most relevant objectives.
- The 'big Ideas' sections from the NCETM 'Teaching for Mastery' documents have been included at the start of each unit. Hyperlinks to the full NCETM 'Teaching for Mastery' documents have also been included for easy reference.
- Hyperlinks to NRich activities have also been added to this version. These are found by clicking on the blue buttons like this one 🛄 at the bottom of relevant objective.
- Some additional content has been added in order to support mixed-aged planning. Any additional content is in *italics*. Occasionally strikethrough has been used to identify when an objective has been altered and this is primarily where an objective has been split between two units.
- Each unit is sub-divided into sections for ease of planning. Sub-categories in this unit are;
 - 1. Recognising and Finding Fractions
 - 2. Decimals
 - 3. Finding and Using Equivalence
 - 4. Calculating with Fractions, Decimals and Percentages
 - 5. Solving Problems

	Yr 3	Yr 4	Yr 5	Yr 6
NCETM Teaching for Mastery Questions, tasks and activities to support assessment	The Big Ideas Fractions are equal parts of a whole. Equal parts of shapes do not need to be congruent but need to be equal in area. Decimal fractions are linked to other fractions. The number line is a useful representation that helps children to think about fractions as numbers.	The Big Ideas Fractions arise from solving problems, where the answer lies between two whole numbers. Fractions express a relationship between a whole and equal parts of a whole. Children should recognise this and speak in full sentences when answering a question involving fractions. For example, in response to the question What fraction of the chocolate bar is shaded? the pupil might say Two sevenths of the whole chocolate bar is shaded. Equivalency in relation to fractions is important. Fractions that look very different in their symbolic notation can mean the same thing.	The Big Ideas Representations that may appear different sometimes have similar underlying ideas. For example 1 4, 0.25 and 25% are used in different contexts but are all connected to the same idea.	 The Big Ideas Fractions express a relationship between a whole and equal parts of a whole. Pupils should recognise this and speak in full sentences when answering a question involving fractions. For example, in response to the question 'What fraction of the journey has Tom travelled?' the pupil might respond, 'Tom has travelled two thirds of the whole journey.' Equivalent fractions are connected to the idea of ratio: keeping the numerator and denominator of a fraction in the same proportion creates an equivalent fraction. Putting fractions in place on the number lines helps understand fractions as numbers in their own right. The Big Ideas (Ratio and Proportion) It is important to distinguish between situations with an additive change or a multiplicative change (which involves ratio). For example, if four children have six sandwiches to share and two more children join them, although two more children have been added, the number of sandwiches then needed for everyone to still get the same amount is calculated multiplicatively.
	Teaching for Mastery Year 3	Teaching for Mastery Year 4	Teaching for Mastery Year 5	Teaching for Mastery Year 6





Strand		Yr3	Yr5	Yr6
Recognising and Finding Fractions	Recognise and find fractions	Yr3 Yr4 (Y3 objective) recognise, find and write fractions of a discrete set of objects: unit fractions and non-unit fractions with small denominators Children should be able to recognise and write unit and non-unit fractions of shapes. Unit Fractions. Unit means one. Here are some examples of unit fractions. Image: state sta	Yr5 recognise mixed numbers and improper fractions and convert from one form to the other. Write mathematical statements >1 as a mixed number (e.g. $\frac{3}{5} + \frac{4}{5} = \frac{9}{6} = 1\frac{1}{5}$) How many halves in: $1\frac{1}{2}3\frac{1}{2}9\frac{1}{2}?$ How many quarters in $1\frac{1}{4}2\frac{1}{4}5\frac{1}{4}?$	Yr6 (Y5 extended) recognise mixed numbers and improper fractions and convert from one form to the other $\frac{10}{7} + \frac{13}{7} = \frac{32}{7}$ leading to: $\frac{7}{5} + \frac{5}{3} = \frac{31}{15}$
Recognising and Finding	Recognise and find fractio	 What fraction of this shape is shaded? How do you know? Is there another way that you can describe the fraction? Here are 21 apples. Put a ring around one third of them. One fifth of 60kg Two fifths of 50 litres (Y3 objective) recognise and use fractions as numbers: unit fractions and non-unit fractions with small denominators Position fractions on a number line; eg. mark fractions such as ½, 3 ½ and 2 3/10 on a number line marked from zero to 5 		
		A fraction of each shape is shaded. Match each fraction to the correct place on the number line. One has been done for you.		





		What comes next?	What comes next?	Give an example	Spot the mistake
		6/10, 7/10, 8/10,,	83/100, 82/100, 81/100,,,	of a fraction that is more than three quarters.	Identify and explain mistakes when counting in
		12/10, 11/10,,,	31/100, 41/100, 51/100,,,	Now another example that no one else will	more complex fractional steps
		True or false?	What do you notice?	tnink of.	what do you notice?
		2/10 of 20cm = 2cm	1/10 of 100 = 10	Explain how you know the fraction is more than three quarters.	One thousandth of my money is 31p. How much do I have?
		4/10 of 40cm = 4cm	1/100 of 100 = 1	What do you notice?	What do you notice?
		3/5 of 20cm = 12cm	2/10 of 100 = 20	Find 30/100 of 200	8/5 of 25 = 40
s		Give an example of a fraction that is less than	2/100 of 100 = 2	Find 3/10 of 200	5/4 of 16 = 20
tio		a nair.	How can you use this to work out 6/10 of 200?	What do you notice?	7/6 of 36 = 42
aci		think of.	6/100 of 200?	Can you write any other similar statements?	Can you write similar statements?
ш́ –		Explain how you know the fraction is less than	True or false?		
ing	ing	a half. (draw an image)	1/20 of a metre= 20cm		
pu	M Reason	Put in Order	4/100 of 2 metres = 40cm		
E P		Ben put these fractions in order starting with the smallest. Are they in the correct order?	Give an example of a fraction that is more than a half but less than a whole. Now another		
ar	G	One fifth, one seventh, one sixth	example that no one else will think of.		
sing	ž	What do you notice?	Explain how you know the fraction is more than a half but less than a whole. (draw an image)		
jū		1/10 of 10 = 1	What do you notice?		
Š		2/10 of 10 = 2	Find 4/6 of 24		
Re		3/10 of 10 = 3	Find 2/3 of 24		
		Continue the pattern. What do you notice?	What do you notice? Can you write any other		
		What about 1/10 of 20? Use this to work out 2/10 of 20, etc	similar statements?		
		What do you notice?			
		Find 2/5 of 10			
		Find 4/10 of 10.			
		What do you notice? Can you write any other similar statements?			





als Counting with docimals	<pre>count up and down in tenths: recognise that tenths arise from dividing an object into 10 equal parts and in dividing one-digit numbers or quantities by 10 Children should be able to: • Use decimal notation for tenths • Divide single digits or whole numbers by 10 • Explain how finding 1/10 is the same as dividing by 10 Here is part of a number line. Write in the numbers missing from the two empty boxes.</pre>	count up and down in hundredths; recognise that hundredths arise when dividing an object by a hundred and dividing tenths by ten What does the digit 6 in 3.64 represent? The 4? What is the 4 worth in the number 7.45? The 5? Continue the count 1.91, 1.92, 1.93, 1.94 Suggest a decimal fraction between 4.1 and 4.2 Know how many 10 pence pieces equal £1, how many 1 pence pieces equal £1, how many centimetres make a metre.		
Decima Compare and Order Decimals		compare numbers with the same number of decimal places up to two decimal placesPlace these decimals on a line from 0 to 2:0.3, 0.1, 0.9, 0.5, 1.2, 1.90012Which is lighter: 3.5kg or 5.5kg? 3.72kg or 3.27kg? Which is less: £4.50 or £4.05?Put in order, largest/smallest first:6.2, 5.7, 4.5, 7.6, 5.2, 99, 1.99, 1.2, 2.1Convert pounds to pence and vice versa. For example: Write 578p in £.How many pence is £5.98, £5.60, £7.06, £4.00? Write the total of ten £1 coins and seven 1p coins (£10.07)Write centimetres in metres. For example, write: 125 cm in metres (1.25 metres)	read, write, order and compare numbers with up to three decimal places Write these numbers in order of size, starting with the smallest. 1.01, 1.001, 1.101, 0.11 Put the correct symbol, < or >, in each box. 3.03 □ 3.3 0.37 □ 0.327 Order these numbers: 0.27 0.207 0.027 2.07 2.7	





		Spot the mistake	Spot the mistake	Spot the mistake	
		six tenths, seven tenths, eight tenths, nine	sixty tenths, seventy tenths, eighty tenths, ninety	0.088, 0.089, 1.0	
		tenths, eleven tenths and correct it.	tentns, twenty tentns and correct it.	What comes next?	
			Put the correct symbol	1.173, 1.183, 1.193	
				What do you notice?	
			0.37 0.32	One tenth of £41, One hundredth of £41, One thousandth of £41	
			What needs to be added to 3.23 to give 3.53?	Continue the pattern. What do you notice?	
als	soning		What needs to be added to 3.16 to give 3.2?	0.085 + 0.015 = 0.1 0.075 + 0.025 = 0.1 0.065 + 0.035 = 0.1 Continue the pattern for the next five number sentences.	
iŭ	Rea			True or false?	
Dec	NCETM			0.1 of a kilometre is 1m.0.2 of 2 kilometres is 2m.0.3 of 3 Kilometres is 3m0.25 of 3m is 500cm.	
				2/5 of £2 is 20p	
				Missing symbol	
				Put the correct symbol < or > in each box	
				4.627 4.06	
				12.317 12.31	
				What needs to be added to 3.63 to give 3.13?	
				What needs to be added to 4.652 to give 4.1?	





Finding and Using Equivalence	Equivalent Fractions	recognise and show, using diagrams, equivalent fractions with small denominators Children should be able to: Identify pairs of fractions that total 1. Circle two fractions that have the same value	recognise and show, using diagrams, families of common equivalent fractions Recognise that five tenths ($\frac{5}{10}$) or one half of this diagram is shaded. Recognise that two eighths ($\frac{7}{6}$) or one quarter ($\frac{1}{4}$) of the set of buttons is ringed Image: shade of the set of buttons is ringed	identify, name and write equivalent fractions of a given fraction, represented visually, including tenths and hundredths Circle the equivalent fractions:	use common factors to simplify fractions; use common multiples to express fractions in the same denomination Children should be able to recognise that a fraction such as $\frac{5}{20}$ can be reduced to an equivalent fraction of ½ by dividing both numerator and denominator by the same number [cancelling] They should be familiar with identifying fractions in different units. E.g. what fraction is 20 pence of two pounds? Of four pounds etc
-		compare and order unit fractions, and fractions with the same denominators	1 2 3	compare and order fractions whose denominators are all multiples of the	<u>compare and order fractions, including</u> fractions >1
	Compare & Order	Children should be able to answer questions like: Would you rather have 1/3 of 30 sweets or 1/5 of 40 sweets? Why?		same number Children should be able to circle the two fractions that have the same value, or choose which one is the odd one out and justify their decision. $6/_{10}$, $3/_{5}$, $18/_{20}$, $9/_{15}$	Children should be able to position fractions on a number line; e.g. mark fractions such as $\frac{7}{5}$, $\frac{11}{20}$, $\frac{19}{12}$ on a number line graduated in tenths Answer questions such as: What number is half way between 5 1⁄4 and 5 1⁄2 ? Which is larger, 1⁄3 or 2⁄5? Explain how you know.





			recognise and write decimal equivalents of any number of tenths or hundredths	<u>read and write decimal numbers as</u> <u>fractions (e.g. $0.71 = \frac{71}{100}$</u>	recognise and write decimal equivalents of any number of tenths or hundredths
			Recognise 0.07 is equivalent to $7\!\!\!/_{100}$ and 6.35 is equivalent to 6 $^{35}\!\!\!/_{100~etc}$	What decimal is equal to 25 hundredths?	Recognise 0.07 is equivalent to $7_{\rm 100}$ and 6.35 is equivalent to 6 $^{35}_{\rm 100\ etc}$
			Which of these decimals is equal to $\frac{19}{100}$? 1.9 10.19 0.19 19.1	$4 + \frac{6}{10} + \frac{2}{100} =$	Which of these decimals is equal to $\frac{19}{100}$? 1.9 10.19 0.19 19.1
			Write each of these as a decimal fraction: ${}^{27}\!/_{100}$ Ch de	Children partition decimals using both decimal and fraction notation, for example, recording 6.38 as $6 + \frac{3}{20} + \frac{8}{200}$ and as $6 + \frac{3}{20} + \frac{8}{200}$	Write each of these as a decimal fraction: ${}^{27}\!/_{100}$
			Write the decimal fraction equivalent to:	0.3 + 0.08.	recognise and write decimal equivalents to 1/2: 1/2: 1/2
lce			two tenths and five hundredths; twenty-nine hundredths; fifteen and nine hundredths.	recognise and use thousandths and relate them to tenths, hundredths and	Know that, for example
valer			recognise and write decimal equivalents to <u>1/4: 1/2: 3/4</u>	decimal equivalents Recognise that 0.007 is equivalent to 7_{1000} 6.305 is equivalent to 6305_{100}	0.5 is equivalent to $\frac{1}{2}$, 0.25 is equivalent to $\frac{1}{4}$, 0.75 is equivalent to $\frac{1}{4}$, 0.1 is equivalent to $\frac{1}{10}$
Equi	ecimals	Know that, for ex 0.5 is equivalent 0.75 is equivalent Particularly in the measurement. Write the decima two tenths and fiv hundredths; fiftee	Know that, for example 0.5 is equivalent to $\frac{14}{2}$, 0.25 is equivalent to $\frac{14}{2}$		Particularly in the context of money and measurement.
Jsing	s and De		0.75 is equivalent to $\frac{3}{4}$, 0.1 is equivalent to $\frac{1}{10}$ Particularly in the context of money and		associate a fraction with division to calculate decimal fraction equivalents (e.g. 0.375) for a simple fraction (e.g. ³ / ₈)
and L	-raction		measurement. Write the decimal fraction equivalent to:		Children should be able to find fractions of numbers and quantities:
inding	Ľ		two tenths and five hundredths; twenty-nine hundredths; fifteen and nine hundredths.		 What fraction of £1 is 35p, 170p ? Write ²³/₁₀₀ of 4 kilogrammes in grams What fraction of 1 litre is 413 ml?
LL.					Convert a fraction to a decimal using known
					equivalent fractions:
					 ¼ = 0.25 ⅔ = 0.4
					Explain how much pizza each person would get if they divided 4 pizzas between 5 people, as a fraction and a decimal
					Circle the two fractions that are equivalent to 0.6.
					6⁄10 ¹ ⁄60 ⁶⁰ ⁄100 ¹ ⁄6





Ince Percentages			write percentages as a fraction with denominator 100, and as a decimal. Shade 10% of the grid below – Which is bigger: 65% or ¾? How do you know? What percentage is the same as 7/10? Explain how you know? What is ³¹ /100 as a percentage? Which is a better mark in a test: 61%, or 30 out of 50? How do you know?	recall and use equivalences between simple fractions, decimals and percentages, including in different contexts. Put a ring around the percentage that is equal to three-fifths – 20% 30% 40% 50% 60% This model is made of 20 cubes. What percentage of the model is made from black cubes?
Finding and Using Equivale	Odd one out. Which is the odd one out in each of these trios? 1/2 3/6 5/8 3/9 2/6 4/9 Why?	Odd one out.Which is the odd one out in each of these trio? $s^{3}4$ $9/12$ $4/6$ $9/12$ $10/15$ $2/3$ Why?Complete the pattern by filling in the blank cells in this table: $1/10$ $2/3$ $10/10$ $10/10$ $10/10$ $10/10$ $10/10$ $20/100$ $10/10$ $100/100$ $10/10$ $100/100$ 0.1 0.3 Another and anotherWrite a decimal numbers (to one decimal place) which lies between a half and three quarters? and another, and another,OrderingPut these numbers in the correct order, starting with the smallest. $\frac{1}{4}$ $\frac{3}{4}$ $1/4$	Odd one out.Which is the odd one out in each of these collections of 4 fractions? $6/10$ $3/5$ $18/20$ $9/15$ $30/100$ $3/10$ $6/20$ $3/9$ Put in OrderImran put these fractions in order starting with the smallest. Are they in the correct order?Two fifths, three tenths, four twentieths How do you know?Complete the pattern $\overline{110}$ $2?$ 100 100 100 100 0.71 0.81 $2??$ Another and another write a fraction with a denominator of one hundred which has a value of more than $0.75?$ and another,OrderingPut these numbers in the correct order, starting with the largest. Explain your thinking $7(10, 0.73, 7/100, 0.073, 71%$	Odd one out.Which is the odd one out in each of these collections of 4 fractions? $\frac{3}{4}$ $\frac{9}{12}$ $\frac{26}{36}$ $\frac{1}{5}$ $\frac{6}{25}$ $\frac{6}{25}$ $\frac{6}{30}$ Give an example of a fraction that is greater than 1.1 and less than 1.5. Now another example that no one will think of. Explain how you know.Complete the pattern $\frac{1}{8}$ $\frac{2}{8}$ $\frac{3}{8}$ $\frac{4}{8}$ 0.375 ?????????Another and another Write a unit fraction which has a value of less than 0.5? and another, and another,Ordering Which is larger, $\frac{1}{3}$ or $\frac{2}{5}$? Explain how you know.Put the following amounts in order, starting with the largest.23%, 5/8, 3/5, 0.8











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entages	Calculating with Percentages			recognise the per cent symbol (%) and understand that per cent relates to 'number of parts per hundred' 30% of 60 is □ 30% of □ is 60	 solve problems involving the calculation of percentages (e.g. of measures) such as 15% of 360 and the use of percentages for comparison Find simple percentages of amounts and compare them. For example: A class contains 12 boys and 18 girls. What percentage of the class are girls? What percentage are boys? 25% of the apples in a basket are red. The rest are green. There are 21 red apples. How many green apples are there?
ēro		What do you notice?	What do you notice?	What do you notice?	True or false?
Pe		1/10 + 9/10 = 1	5/5 - 1/5 = 4/5	³ ⁄ ₄ and ¹ ⁄ ₄ = 4/4 = 1	25% of 23km is longer than 0.2 of 20km.
and		2/10 + 8/10 = 1	4/5 - 1/5 = 3/5	4/4 and ¼ = 5/4 = 1 ¼	Convince me.
IIS 8		3/10 + 7/10 = 1	Continue the pattern	$5/4$ and $\frac{1}{4} = 6/4 = 1\frac{1}{2}$	Another and another
ma		Continue the pattern	Can you make up a similar pattern for addition?	Continue the pattern up to the total of 2.	Write down two fractions which have a difference
eci		Can you make up a similar pattern for eighths?	The answer is 3/5, what is the question?	Can you make up a similar pattern for subtraction?	Another and another
Calculating with Fractions, Deci	NCETM Reasoning	Can you make up a similar pattern for eighths? The answer is 5/10, what is the question? (involving fractions / operations)	The answer is 3/5, what is the question? What do you notice? 11/100 + 89/100 = 1 12/100 + 88/100 = 1 Continue the pattern for the next five number sentences	Can you make up a similar pattern for subtraction? The answer is 1 2/5 , what is the question Continue the pattern $\frac{1}{4} \times 3 =$ $\frac{1}{4} \times 4 =$ $\frac{1}{4} \times 5 =$ Continue the pattern for five more number sentences. How many steps will it take to get to 3? $\frac{5}{3}$ of $24 = 40$ Write a similar sentence where the answer is $\frac{5}{6}$. The answer is 2 $\frac{1}{4}$, what is the question Give your top tips for multiplying fractions. Which is more: $\frac{20\% of 200 or 25\% of 180?}{2}$ Explain your reasoning.	of 1 2/ and another, and another, Another and another Write down 2 fractionswith a total of 3 4/5 and another, and another, Continue the pattern What do you notice? $1/3 \div 2 = 1/6$ $1/6 \div 2 = 1/12$ $1/12 \div 2 = 1/24$ Give your top tips for dividing fractions. What else do you know? 88% of a sum of money = £242. Make up some other statements. Write real life problems for your number sentences. Undoing I think of a number and then reduce it by 15%. The number I end up with is 306. What was my original number? In a sale where everything is reduced by 15% I paid the following prices for three items. What was the original selling price?
				- Aprilling of todoor in g.	faid the following prices for three items was the original selling price? £255, £850, £4.25









Solving Problems	A box of four balls costs £2.96. How much does each ball cost? Dean and Alex buy 3 boxes of balls between them. Dean pays £4.50. How much must Alex pay? A full bucket holds 5½ litres A full bucket holds ½ litres A full jug holds ½ a litre. How many jugs full of water will fill the bucket? Max jumped 2.25 metres on his second try at	
	Max jumped 2.25 metres on his second try at the long jump.	
	This was 75 centimetres longer than on his first try.	
	How far in metres did he jump on his first try?	



