#### Unit Overview and Guidance

- The exemplification has been taken from the NCETM online 'Resource Toolkit', with additions in order to ensure full coverage.
- Links to the White Rose Maths hubs schemes of work (with questions categorised into the three aims of the national curriculum i.e. fluency, problem solving and reasoning) are hyperlinked to each of the objectives. Many thanks go to the White Rose Maths hub for permission to include their resources.
- The NCETM reasoning questions have also been incorporated into each unit and are identified in pale purple boxes underneath the group of the most relevant objectives.
- The 'big Ideas' sections from the NCETM 'Teaching for Mastery' documents have been included at the start of each unit. Hyperlinks to the full NCETM 'Teaching for Mastery' documents have also been included for easy reference.
- Hyperlinks to NRich activities have also been added to this version. These are found by clicking on the blue buttons like this one 🛄 at the bottom of relevant objective.
- Some additional content has been added in order to support mixed-aged planning. Any additional content is in *italics*. Occasionally strikethrough has been used to identify when an objective has been altered and this is primarily where an objective has been split between two units.
- Each unit is sub-divided into sections for ease of planning. Sub-categories in this unit are;
  - 1. Recognising and Finding Fractions
  - 2. Decimals
  - 3. Finding and Using Equivalence
  - 4. Calculating with Fractions, Decimals and Percentages
  - 5. Solving Problems

	Yr 3	Yr 4	Yr 5	Yr 6
NCETM Teaching for Mastery Questions, tasks and activities to support assessment	The Big Ideas Fractions are equal parts of a whole. Equal parts of shapes do not need to be congruent but need to be equal in area. Decimal fractions are linked to other fractions. The number line is a useful representation that helps children to think about fractions as numbers.	The Big Ideas Fractions arise from solving problems, where the answer lies between two whole numbers. Fractions express a relationship between a whole and equal parts of a whole. Children should recognise this and speak in full sentences when answering a question involving fractions. For example, in response to the question What fraction of the chocolate bar is shaded? the pupil might say Two sevenths of the whole chocolate bar is shaded. Equivalency in relation to fractions is important. Fractions that look very different in their symbolic notation can mean the same thing.	The Big Ideas Representations that may appear different sometimes have similar underlying ideas. For example 1 4, 0.25 and 25% are used in different contexts but are all connected to the same idea.	<ul> <li>The Big Ideas</li> <li>Fractions express a relationship between a whole and equal parts of a whole. Pupils should recognise this and speak in full sentences when answering a question involving fractions. For example, in response to the question 'What fraction of the journey has Tom travelled?' the pupil might respond, 'Tom has travelled two thirds of the whole journey.'</li> <li>Equivalent fractions are connected to the idea of ratio: keeping the numerator and denominator of a fraction in the same proportion creates an equivalent fraction.</li> <li>Putting fractions in place on the number lines helps understand fractions as numbers in their own right.</li> <li>The Big Ideas (Ratio and Proportion)</li> <li>It is important to distinguish between situations with an additive change or a multiplicative change (which involves ratio). For example, if four children have six sandwiches to share and two more children join them, although two more children have been added, the number of sandwiches then needed for everyone to still get the same amount is calculated multiplicatively.</li> </ul>
	Teaching for Mastery Year 3	Teaching for Mastery Year 4	Teaching for Mastery Year 5	Teaching for Mastery Year 6





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and non-unit fractions with small denominators       fractions and convert from one form to       improper fractions and convert from one form to         Children should be able to recognise and write unit and non-unit fractions of shapes.       >1 as a mixed number       form to the other	Strand	Yr3 Yr4	Yr5	Yr6
Unit Fractions. Unit means one. Here are some examples of unit fractions.	and Finding Fractions	<ul> <li>Y13 objective) recognise, find and write fractions of a discrete set of objects: unit fractions and non-unit fractions with small denominators</li> <li>Children should be able to recognise and write unit and non-unit fractions of shapes.</li> <li>Unit Fractions. Unit means one. Here are some examples of unit fractions.</li> <li>Image: Participation of the state of the st</li></ul>	recognise mixed numbers and improper fractions and convert from one form to the other. Write mathematical statements >1 as a mixed number(e.g. $\frac{2}{5} + \frac{4}{5} = \frac{6}{5} = 1\frac{1}{5}$ )How many halves in: $1\frac{1}{2}3\frac{1}{2}9\frac{1}{2}?$ How many quarters in $1\frac{1}{4}2\frac{1}{4}5\frac{1}{4}?$	(Y5 extended) recognise mixed numbers and improper fractions and convert from one form to the other $\frac{10}{7} + \frac{13}{7} = \frac{32}{7}$ leading to:





		What comes next?	What comes next?	Give an example	Spot the mistake
		6/10, 7/10, 8/10,,	83/100, 82/100, 81/100,,,	of a fraction that is more than three quarters.	Identify and explain mistakes when counting in
		12/10, 11/10,,,	31/100, 41/100, 51/100,,,	Now another example that no one else will	more complex fractional steps
		True or false?	What do you notice?	think of.	What do you notice?
		2/10 of 20cm = 2cm	1/10 of 100 = 10	Explain how you know the fraction is more than three quarters.	One thousandth of my money is 31p. How much do I have?
		4/10 of 40cm = 4cm	1/100 of 100 = 1	What do you notice?	What do you notice?
		3/5 of 20cm = 12cm	2/10 of 100 = 20	Find 30/100 of 200	8/5 of 25 = 40
S		Give an example of a fraction that is less than	2/100 of 100 = 2	Find 3/10 of 200	5/4 of 16 = 20
tior		a half.	How can you use this to work out 6/10 of 200?	What do you notice?	7/6 of 36 = 42
Fractions		Now another example that no one else will think of.	6/100 of 200?	Can you write any other similar statements?	Can you write similar statements?
		Explain how you know the fraction is less than	True or false?		
Finding	ing		1/20 of a metre= 20cm		
pd	ason	Put in Order	4/100 of 2 metres = 40cm		
and Fi	M Rea	Ben put these fractions in order starting with the smallest. Are they in the correct order?	Give an example of a fraction that is more than a half but less than a whole. Now another		
ar	CET	One fifth, one seventh, one sixth	example that no one else will think of.		
Recognising	NCI	What do you notice?	Explain how you know the fraction is more than a half but less than a whole. (draw an image)		
gui		1/10 of 10 = 1	What do you notice?		
°,		2/10 of 10 = 2	Find 4/6 of 24		
Re		3/10 of 10 = 3	Find 2/3 of 24		
		Continue the pattern. What do you notice?	What do you notice? Can you write any other		
		What about 1/10 of 20? Use this to work out 2/10 of 20, etc	similar statements?		
		What do you notice?			
		Find 2/5 of 10			
		Find 4/10 of 10.			
		What do you notice? Can you write any other similar statements?			





lais	<ul> <li>count up and down in tenths: recognise that tenths arise from dividing an object into 10 equal parts and in dividing one-digit numbers or quantities by 10</li> <li>Children should be able to:         <ul> <li>Use decimal notation for tenths</li> <li>Divide single digits or whole numbers by 10</li> <li>Explain how finding 1/10 is the same as dividing by 10</li> <li>Here is part of a number line. Write in the numbers missing from the two empty boxes.</li> </ul> </li> </ul>	count up and down in hundredths; recognise that hundredths arise when dividing an object by a hundred and dividing tenths by ten What does the digit 6 in 3.64 represent? The 4? What is the 4 worth in the number 7.45? The 5? Continue the count 1.91, 1.92, 1.93, 1.94 Suggest a decimal fraction between 4.1 and 4.2 Know how many 10 pence pieces equal £1, how many 1 pence pieces equal £1, how many centimetres make a metre.		
Decimals	Compare and Order Decimals	compare numbers with the same number of decimal places up to two decimal placesPlace these decimals on a line from 0 to 2: 0.3, 0.1, 0.9, 0.5, 1.2, 1.9Image: Colspan="2">Image: Colspan="2">Image: Colspan="2">Colspan="2">Colspan="2">Colspan="2">Colspan="2">Colspan="2">Colspan="2">Colspan="2"	read, write, order and compare numbers         with up to three decimal places         Write these numbers in order of size, starting with the smallest. 1.01, 1.001, 1.101, 0.11         Put the correct symbol, < or >, in each box.         3.03 □ 3.3         0.37 □ 0.327         Order these numbers: 0.27 0.207 0.027 2.07         2.7	





		Spot the mistake	Spot the mistake	Spot the mistake	
		six tenths, seven tenths, eight tenths, nine	sixty tenths, seventy tenths, eighty tenths, ninety	0.088, 0.089, 1.0	
		tenths, eleven tenths and correct it.	tenths, twenty tenths and correct it.	What comes next?	
			Missing symbol	1.173, 1.183, 1.193	
			Put the correct symbol < or > in each box	What do you notice?	
			3.03 3.33	One tenth of £41, One hundredth of £41,	
			0.37 0.32	One thousandth of £41	
			What needs to be added to 3.23 to give 3.53?	Continue the pattern. What do you notice?	
als	asoning		What needs to be added to 3.16 to give 3.2?	0.085 + 0.015 = 0.1 0.075 + 0.025 = 0.1 0.065 + 0.035 = 0.1 Continue the pattern for the next five number sentences.	
<u>ü</u>	Rea			True or false?	
Decimals	NCETM I			<ul> <li>0.1 of a kilometre is 1m.</li> <li>0.2 of 2 kilometres is 2m.</li> <li>0.3 of 3 Kilometres is 3m</li> <li>0.25 of 3m is 500cm.</li> </ul>	
				2/5 of £2 is 20p	
				Missing symbol	
				Put the correct symbol < or > in each box	
				4.627 4.06	
				12.317 🔲 12.31	
				What needs to be added to 3.63 to give 3.13?	
				What needs to be added to 4.652 to give 4.1?	





Finding and Using Equivalence		Image: second secon	identify, name and write equivalent fractions of a given fraction, represented visually, including tenths and hundredths Circle the equivalent fractions: $\frac{7}{100}$ $\frac{100}{7}$ $\frac{2}{5}$ $\frac{40}{100}$ Now find one more example with shapes	Use common factors to simplify fractions; use common multiples to express fractions in the same denomination Children should be able to recognise that a fraction such as $\frac{5}{20}$ can be reduced to an equivalent fraction of ½ by dividing both numerator and denominator by the same number [cancelling] They should be familiar with identifying fractions in different units. E.g. what fraction is 20 pence of two pounds? Of four pounds etc
Compare & Order	compare and order unit fractions, and fractions with the same denominators         Children should be able to answer questions like:         Would you rather have 1/3 of 30 sweets or 1/5 of 40 sweets? Why?		compare and order fractions whose denominators are all multiples of the same number Children should be able to circle the two fractions that have the same value, or choose which one is the odd one out and justify their decision. $6/_{10}$ , $3/_{5}$ , $18/_{20}$ , $9/_{15}$	compare and order fractions, including fractions >1Children should be able to position fractions on a number line; e.g. mark fractions such as $\frac{7}{5}$ , $\frac{11}{20}$ , $\frac{18}{12}$ on a number line graduated in tenthsAnswer questions such as:What number is half way between 5 ½ and 5 ½ ?Which is larger, ½ or $\frac{2}{5}$ ? Explain how you know.





		recognise and write decimal equivalents of any number of tenths or hundredths	read and write decimal numbers as fractions (e.g. $0.71 = \frac{71}{100}$	recognise and write decimal equivalents of any number of tenths or hundredths
		Recognise 0.07 is equivalent to $7\!\!\!/_{100}$ and 6.35 is equivalent to 6 $^{35}\!\!/_{100~etc}$	What decimal is equal to 25 hundredths? Write the total as a decimal:	Recognise 0.07 is equivalent to $7_{\rm 100}$ and 6.35 is equivalent to 6 $^{35}\!\!\!\!\!\!/_{\rm 100\ etc}$
		Which of these decimals is equal to $^{19}/_{100}$ ? 1.9 10.19 0.19 19.1	$4 + \frac{6}{10} + \frac{2}{100} =$	Which of these decimals is equal to $\frac{19}{100}$ ? 1.9 10.19 0.19 19.1
		Write each of these as a decimal fraction: ${}^{27}\!\!/_{100}$	Children partition decimals using both decimal and fraction notation, for example, recording 6.38 as $6 + \frac{3}{10} + \frac{9}{100}$ and as $6 + \frac{3}{100} + \frac{9}{100}$	Write each of these as a decimal fraction: $^{27}\!\!\!/_{100}$ $^{37}\!\!\!/_{100}$ 2 $^{33}\!\!\!/_{100}$
		Write the decimal fraction equivalent to:	0.3 + 0.08.	recognise and write decimal equivalents to <i>¼</i> ; <i>½</i> ; <i>¾</i>
e		two tenths and five hundredths; twenty-nine hundredths; fifteen and nine hundredths.	recognise and use thousandths and relate them to tenths, hundredths and	Know that, for example
alen		recognise and write decimal equivalents to $\frac{1}{14}$ ; $\frac{1}{2}$ ; $\frac{3}{4}$	decimal equivalents	0.5 is equivalent to $\frac{1}{2}$ , 0.25 is equivalent to $\frac{1}{4}$ ,
Equivalence	<u>a</u>	Know that, for example	Recognise that 0.007 is equivalent to $7/_{1000}$	0.75 is equivalent to $\frac{3}{10}$ , 0.1 is equivalent to $\frac{1}{10}$ Particularly in the context of money and
	and Decimal	0.5 is equivalent to $\frac{1}{2}$ , 0.25 is equivalent to $\frac{1}{4}$ ,	6.305 is equivalent to <sup>6305</sup> /100	measurement.
Using		0.75 is equivalent to $\frac{3}{4}$ , 0.1 is equivalent to $\frac{1}{10}$ Particularly in the context of money and		associate a fraction with division to calculate decimal fraction equivalents (e.g. 0.375) for a simple fraction (e.g. 3/6)
and L	actions	measurement. Write the decimal fraction equivalent to:		Children should be able to find fractions of numbers and quantities:
Finding a	ι	two tenths and five hundredths; twenty-nine hundredths; fifteen and nine hundredths.		<ul> <li>What fraction of £1 is 35p, 170p ?</li> <li>Write <sup>23</sup>/<sub>100</sub> of 4 kilogrammes in grams</li> <li>What fraction of 1 litre is 413 ml?</li> </ul>
ι.				Convert a fraction to a decimal using known
				equivalent fractions:
				<ul> <li>¼ = 0.25</li> <li>¾ 5 = 0.4</li> </ul>
				Explain how much pizza each person would get if they divided 4 pizzas between 5 people, as a fraction and a decimal
				Circle the two fractions that are equivalent to 0.6.
				6/10 <sup>1</sup> /60 <sup>60</sup> /100 <sup>1</sup> /6





Ince			write percentages as a fraction with denominator 100, and as a decimal.         Shade 10% of the grid below –         Which is bigger: 65% or ¾? How do you know?         What percentage is the same as 7/10?         Explain how you know?         What is <sup>3</sup> / <sub>100</sub> as a percentage?         Which is a better mark in a test: 61%, or 30 out of 50? How do you know?	recall and use equivalences between simple fractions, decimals and percentages, including in different contexts.         Put a ring around the percentage that is equal to three-fifths – 20% 30% 40% 50% 60%         This model is made of 20 cubes.         What percentage of the model is made from black cubes?
Finding and Using Equivalence	Odd one out. Which is the odd one out in each of these trios? 1/2 3/6 5/8 3/9 2/6 4/9 Why?	Odd one out.Which is the odd one out in each of these trio? $s^{3}4$ $9/12$ $4/6$ $9/12$ $10/15$ $2/3$ Why?Complete the pattern by filling in the blank cells in this table: $10$ $10$ $10$ $10$ $20$ $40$ $100$ $100$ $100$ $0.1$ $0.3$ $100$ Another and anotherWrite a decimal numbers (to one decimal place) which lies between a half and three quarters? and another, and another,OrderingPut these numbers in the correct order, starting with the smallest. $\frac{1}{4}$ $0.75$ $5/10$ $4/8$ $\frac{3}{4}$ $1/4$	Odd one out.Which is the odd one out in each of these collections of 4 fractions? $6/10$ $3/5$ $18/20$ $9/15$ $30/100$ $3/10$ $6/20$ $3/9$ Put in OrderImran put these fractions in order starting with the smallest. Are they in the correct order?Two fifths, three tenths, four twentieths How do you know?Complete the patternImage: Complete the patternImage: One hundred which has a value of more than $0.75? \dots$ and another, $\dots$ and another, $\dots$ OrderingPut these numbers in the correct order, 	Odd one out.Which is the odd one out in each of these collections of 4 fractions? $\frac{3}{4}$ $\frac{9}{12}$ $\frac{26}{36}$ $\frac{15}{6}$ $\frac{6}{25}$ $\frac{1}{2}$ $\frac{3}{2}$ $\frac{1}{2}$ $\frac{3}{2}$ $\frac{3}{2}$ $\frac{3}{2}$ $\frac{1}{2}$ <tr< td=""></tr<>











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Calculating with Percentages			recognise the per cent symbol (%) and understand that per cent relates to 'number of parts per hundred' 30% of 60 is □ 30% of □ is 60	<ul> <li>solve problems involving the calculation of percentages (e.g. of measures) such as 15% of 360 and the use of percentages for comparison</li> <li>Find simple percentages of amounts and compare them. For example:</li> <li>A class contains 12 boys and 18 girls. What percentage of the class are girls? What percentage are boys?</li> <li>25% of the apples in a basket are red. The rest are green. There are 21 red apples. How many green apples are there?</li> </ul>
	What do you notice?	What do you notice?	What do you notice?	True or false?
	1/10 + 9/10 = 1	5/5 - 1/5 = 4/5	<sup>3</sup> ⁄ <sub>4</sub> and <sup>1</sup> ⁄ <sub>4</sub> = 4/4 = 1	25% of 23km is longer than 0.2 of 20km.
aud	2/10 + 8/10 = 1	4/5 - 1/5 = 3/5	4/4 and ¼ = 5/4 = 1 ¼	Convince me.
	3/10 + 7/10 = 1	Continue the pattern	$5/4$ and $\frac{1}{4} = 6/4 = 1\frac{1}{2}$	Another and another
	Continue the pattern	Can you make up a similar pattern for addition?	Continue the pattern up to the total of 2.	Write down two fractions which have a difference of 1 2/ and another, and another,
	Can you make up a similar pattern for eighths?	The answer is 3/5, what is the question?	Can you make up a similar pattern for subtraction?	Another and another
	The answer is 5/10, what is the question? (involving fractions / operations)	What do you notice?	The answer is 1 2/5, what is the question	Write down 2 fractionswith a total of 3 4/5
		11/100 + 89/100 = 1	Continue the pattern	and another, and another,
		12/100 + 88/100 = 1	¼ x 3 =	Continue the pattern What do you notice?
Aurig with Fis		13/100 + 87/100 = 1	¼ x 4 =	$1/3 \div 2 = 1/6$
nun easo		Continue the pattern for the next five number sentences	¼ x 5 =	$1/6 \div 2 = 1/12$
≶  ະັ ⊂ ר			Continue the pattern for five more number	$1/12 \div 2 = 1/24$
			sentences. How many steps will it take to get to 3?	Give your top tips for dividing fractions.
ž d			5/3  of  24 = 40	What else do you know?
			Write a similar sentence where the answer is 56.	88% of a sum of money = £242. Make up some other statements. Write real life problems for your number sentences.
			The answer is 2 ¼ , what is the question	Undoing
			Give your top tips for multiplying fractions. Which is more:	I think of a number and then reduce it by 15%. The number I end up with is 306. What was my
			20% of 200 or 25% of 180?	original number?
			Explain your reasoning.	In a sale where everything is reduced by 15% I paid the following prices for three items. What was the original selling price?
				£255, £850, £4.25









Problems		A box of four balls costs £2.96. How much does each ball cost? Dean and Alex buy 3 boxes of balls between them. Dean pays £4.50. How much must Alex pay? A full bucket holds 5½ litres	
Solving Pro		A full jug holds 1/2 a litre. How many jugs full of	
		A full jug holds ½ a litre. How many jugs full of water will fill the bucket?	
		Max jumped <b>2.25 metres</b> on his <b>second</b> try at the long jump.	
		This was <b>75 centimetres</b> longer than on his <b>first</b> try.	
		How far in metres did he jump on his first try?	



